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DECISION MAKING IN WATER RESOURCES PLANNING FOR SAUDI ARABIA

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ABSTRACT

A quantitative survey on the availability of ground and surface water in various regions of Saudi Arabia is carried out and the anticipated future demands are reviewed. Alternate feasible water development plans are eval uated to meet the increasing demands in various sectors. Demand relationships with time are established. Cost-capacity relationships for the selected sources are developed. An optimization scheme based on dynamic programming principles is formulated and applied to determine when and how much capacity should be added to the system to meet future demands.

INTRODUCTION

The need for treated water in the kingdom is expected to increase manyfold in the next two decades due to anticipated high growth rate of the urban population, improvements in the standard of living, and rapid industr ial and agricultural development. To meet such demands, water resource development plans at the national and regional levels were prepared by the Ministry of Agriculture and Water [20]. The main objective of these plans is to ensure the supply of adequate quantities of potable water of acceptable standards for urban, industrial and agricultural developments. Dams to collect surface waters for both agricultural and recharge purposes are also being planned and constructed.

This paper presents an overview of the available ground and surface water resources and anticipated water demands in different sectors for the next two decades. Demand forecasting models are developed and the economics of water resource alternatives is studied. A methodology using dynamic programming principle is formulated and applied to optimize the expansion of the water resources system.

WATER RESOURCES IN SAUDI ARABIA-AN OVERVIEW

Many studies have been conducted in the past to evaluate the available ground and surface water resources in the Kingdom of Saudi Arabia $[1,6,10,11,$ 16,17,19,20]. Among these, the national water balance study presented in the Third Development Plan [20] is the most comprehensive and most recent. The principal water consumers in this study are categorized as (a) residential, commercial and industrial consumers; (b) rural consumers including livestock;

and (c) agricultural consumers.

For management procedures, the Ministry of Agriculture and Water has divided the Kingdom into five water resources regions. These are: eastern, northern, central, western and south western regions. The boundaries of these regions are delineated on the basis of the availability of groundwater resources in each region, aquifer characteristics, existing and planned regional developments and distinct hydrological conditions. In each region four alternative water resources are suggested. These are; renewable resources, non-renewable resources, desalination, and reclamation from waste waters. Table 1 summarizes the water budget statistics for each alternative on a regional basis [20].

An evaluation of these alternatives shows that the western region is the most critical where future water demands are expected to be high. To meet such demands, desalination expansion is recommended as the most feasible water supply source.

Reclaimed water from urban waste waters is also suggested as a potential source for agricultural and industrial needs. Water will be reclaimed from urban waste waters particularly from cities with population over 100,000. These cities, at present, are: Riyadh, Jeddah, Dammam Metropolitan Area, Makkah, Al-Madinah, Taif, and Hofuf. It is anticipated that the reclaimed water will contribute the equivalent of 15% of the Kingdom's known conven tional resources. Due to large proven ground water reserves in the central and northern regions, the shortage in these regions is not very critical since these reserves can easily be utilized to supply water to over 40% of the Kingdom's irrigated areas projected for the next 20 years [20].

WATER DEMAND FORECASTING MODELS

Water utilization data listed in Table 1 were used to develop simple water demand models. The coefficient of correlation was also computed to test the model validity. The demand forecasting model developed in this study is based on the following exponential equation.

$$
D_t = a e^{b \cdot t} \tag{1}
$$

where,

- D_r is the estimated water requirements in million cubic meter/year at time t in different regions;
	- t is the time in years (t=0, at year 1399 H)
	- a and b are regression coefficients determined statistically from water utilization data.

In order to test the validity of the previous equation, the correlation coefficient $'\rho^{2}$ was also computed. The regression coefficients and the respective correlation coefficients for each resource and area are listed in

TABLE 1 - NATIONAL WATER BALANCE [20]

 $\sqrt{2}$

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(million cubic meters per year)

 $\sqrt{2}$

Table 2. In all cases, except for the agricultural sector, the correlation coefficient ' p^2 ' is above 0.90. This implies that an exponential regression model similar to Equation (1) is suitable for forecasting demands in all sectors except in irrigated agriculture. The coefficient 'a' in Table 2 indicates the initial demand and 'b' the growth rate. The negative values of 'b' in the water forecasting model for the surplus mean that the surplus water is being utilized with time thus showing an improvement towards better water resources management.

A similar study on demand forecasting was conducted for major cities in Saudi Arabia. The cities selected were Jeddah, Riyadh, Dammam and Makkah. Based on the estimated annual demand data for these cities [2], the parameters of the demand forecasting model were computed and are listed in Table 3. It is found that the demand growth factor 'b' for Makkah, which is 0.1142, is relatively high compared to other cities where it varies from .055 to 0.082.

COST-CAPACITY RELATIONSHIP

Due to the lack of cost information on other alternatives, the cost evaluation made in this section is restricted to desalination only. The total cost of water supplied by a desalination system consists of the capital costs, variable operating costs, and the annual fixed operating and mainten ance costs. The capital and fixed operations and maintenance costs are a function of the plant capacity while the variable costs are a function of the current output rate of the plant.

Using data listed in Table 4 on multi-stage flash evaporation (MSF) plants installed in Saudi Arabia, a cost-capacity relationship was estab lished as follows:

$$
C_c = 43200 \, (X)^{0.751} \tag{2}
$$

where,

 C_{\sim} is the capital cost in SR/m³/day; and X is the capacity in thousand m^3 /day.

Due to the lack of information on annual operations and maintenance costs for different MSF plants installed in Saudi Arabia, this cost-component could not be expressed as a function of capacity. However, a value of 24% of the known capital cost is suggested by Larson et al $[12]$. These relationships could be used in optimizing system expansion.

OPTIMAL EXPANSION OF WATER RESOURCES SYSTEM

As revealed in Table 1, water demand in each sector increases exponen tially with time. To meet these demands, the planning of water supply ideally should consider the optimal timing and size of the additional plant capacity. Water resources planners and decision makers are faced with such critical issues since the expansion of these utility services generally depends upon

TABLE 2 - WATER DEMAND FORECASTING MODELS FOR SAUDI ARABIA*

* Type of model used is = $D_t = ae^{bt}$ where, $\texttt{D}_{\texttt{t}}$ is demand in million cubic meter per year at time t $t = 0$ at 1399H and

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= 1 at 1400H etc

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TABLE 3 - URBAN WATER DEMAND FORECASTING MODELS^{*} FOR

SELECTED MAJOR CITIES IN SAUDI ARABIA

Demands in thousands cubic meter per day

 $\ddot{}$ **/'** TABLE 4 - COST EVALUATION OF SCME MSF DESALINATION PLANTS IN SAUDI ARABIA [22]

a number of factors such as growth rate, expected economic life of the utility, economies of scale, annual discount rates on the investment and rate of interest on bonds issued for the utility construction.

To accomplish the objective of optimal capacity expansion in the field of water resources planning, mathematical optimization techniques have been applied in the past [2, 4, 5, 8, 9, 13, 15, 18, 22]. Scarato [18] has presented a minimum cost method to determine optimum timings and size compo nents to meet future water demand. In other studies, the dynamic programming technique has been used in deciding the optimal sequences for the construction of water supply projects [5, 15]. Hinomoto [8] has developed a multi-stage capacity expansion model that is used to expand municipal water treatment systems. Zukovs et al [22] have used a dynamic programming formulation for optimal capacity expansion of wastewater treatment plants servicing sewerage system.

This section briefly describes the application of dynamic programming in the expansion of water supply systems to meet domestic and industrial demands in urban areas. The methodology presented in this study is restricted to the expansion of water supply systems based on desalination only. However, it can be modified for expanding desalination processes used in conjunction with available ground and surface water resources [7, 14].

Dynamic programming is a mathematical technique which is useful for making a sequence of interrelated decisions [3]. Formulations, using this technique, require decomposition of the state and decision variables into a number of stages. At each stage, a policy decision is made which then transforms the current state into a state associated with the next stage.

In this study, the total capacity needed for a planning period 'T' is the stale variable. Each one year interval is a single stage with a total of 'T' stages. The decision variables involved are the capacity increment and the time. The total true cost at the beginning of a time period is the summation of the discounted cost of capacity increment ${^\prime}{\rm X}_{\bf t\, ,s}^{}$ and the optimal discounted cost of system expansion at the beginning of period 's+1' to meet demand up to the end of planning period 'T'. The objective here is to mini mize the total discounted cost which can be mathematically represented by the following equation:

$$
f_{t}^{*}(X_{t,T}) = Min [C(X_{t,s}) + (1+r)^{-(s-t)} f_{s}^{*}(X_{t,T} - X_{t,s})]
$$
\n
$$
X_{t,s}
$$
\n
$$
t \in T \begin{bmatrix} t = 1, 2, ..., T \\ s = t, t+1, ..., T \end{bmatrix}
$$
\n(3)

where,

 $f_t^*(X_{t,T})$ is the minimum discounted sum of capital and opertating costs for the desalination plants installed in beginning of year $'t'$ and thereafter to meet water demand;

 $X_{t,s}$ is capacity increment between beginning of period 't' and end of period 's';

 $C(X_{t,s})$ is the discounted capital and operating costs for capacity increment $\mathbf{x}_{\mathsf{t},\mathsf{s}}'$ and is discounted to the beginning of period $'t$:

 $X_{t,T}$ is the total water demand from the beginning of period t to the end of period T;

is the discount rate; and

 $f_s^*(X_{t,T}-X_{t,s})$ is the minimum discounted capital and operating costs for the system to meet demands in year s and thereafter.

All costs in the above equation (3) are discounted to the beginning of year 't'.

Using the backward dynamic programming algorithm, the initial condition is defined as follows:

At period 'T',

$$
f_{T}^{*}(X_{T,T}) = Min [C(X_{T,T})] = C(X_{T,T})
$$
 (4)

Knowing the optimum value at the period 'T', the recursive equation at period T-l can be written as follows:

$$
f_{T-1}^{*}(X_{T,T}) = Min \qquad \qquad \begin{bmatrix} c(x_{T-1, T-1}) + (1+r)^{-1} f_{T}^{*}(X_{T-1, T}X_{T-1, T-1}) \\ c(x_{T-1, T}) \end{bmatrix}
$$
 (5)

Similarly, the generalized recursive equation at 't' can be expanded using all possible combinations of 's' and 't' in Equation (3).

The capital and operating costs discounted to the beginning of period 't' as a function of plant capacity $X_{t,s}$ are computed using the following algorithm:

1. Capacity $X_{t,s}$ is computed as follows:

$$
X_{t,s} = D_s - D_{t-1} \tag{6}
$$

where,

 D_{S} is the total water demand at the end of period 's'; and D is the total water demand up to the beginning of period 't' or the end of period t-l; These demands can be computed using the water forecasting model of

Equation (1).

- 2. For any desalination process under consideration, the capital cost $C_c(X_{t,s})$ for capacity $X_{t,s}$, is computed using the derived capital cost-capacity relationships. Similarly the annual fixed operating cost, $C_f(X_{t,s})$ is computed using an operating cost-capacity relationship if available, otherwise it may be determined as a percentage of the total capital cost.
- 3. The variable operating cost $C_v(X_{t,s}U_r)$ depends upon the capacity and the plant usage rate U_r . This rate increases annually for a given plant from period 't' through period 's' and stays constant indefin itely thereafter at the maximum value. Due to lack of data on plant use-rates, this cost component has not been considered separately in the present study.

4. The total discounted cost
$$
C(X_{t,s})
$$
 is computed as follows [8]:

$$
C(X_{t,s}) = (\frac{1+r}{r}) \alpha C_c(X_{t,s}) + \frac{\sqrt{1+r}}{r} C_f(X_{t,s})
$$
(7)

where,

- r is the discount rate
- is the amorization factor and is a function of the $\alpha = \frac{i}{1-(1+i)^{-n}}$

function of the interest rate 'i' and plant life 'n' years.

ILLUSTRATIVE EXAMPLE

Considering the case of desalination expansion in the western region of the Kingdom of Saudi Arabia (Table 1) for a planning period, T = 10 years, the expansion of desalination to meet the demand in the region is expressed by the following equation:

$$
D_t = 201e^{-1246} t \tag{8}
$$

where,

 D_t = Amount of water to be supplied by desalination in 1000 m³/day at time t (t=0 at 1399H).

The other factors assumed in this study are: discount rate, $r = 10\%$; interest rate, $i = 5\%$; and plant life $n = 20$ years.

The cost capacity relationship for the desalination plants installed or proposed in the Kingdom of Saudi Arabia, as given in Equation (2), is rewritted for the period t>s as:

$$
C_c(X_{t,s}) = 43200 (X_{t,s})^{0.751}
$$
 (9)

where,

 $C_c(X_{t,s})$ is the capital cost in SR/m³/day.

TABLE 5 - CAPACITY INCREMENT $x_{t,s}$ installed at the beginning of YEAR 't' TO MEET DEMAND THROUGH 's' (THOUSANDS m^3/DAY) $\mathbf 1$ $\frac{1}{4}$ 6 $\overline{2}$ $\overline{3}$ $\overline{7}$ $\bf8$ $\overline{9}$ ${\bf s}$ t. 103 147 197 253 317 390 472 564 73 117 167 223 287 359 141 534 83 133 189 253 325 407 500 94 150 214 286 368 461 106 170 242 324 417 120

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TABLE 6 - THE TOTAL DISCOUNTED COST C(X_{t,S}) (MILLION SR)

 $X_{t,s}$ is the capacity in thousand m³/day.

The average annual operating cost is taken at 24% of the capital cost [12].

Using the above data, the capacity increment, $\mathbf{x}_{\mathsf{t},\mathbf{s}}^{},$ and the associated total discounted costs $\mathsf{C}(\mathsf{X}_{\mathsf{t},\mathsf{s}}^{\bullet})$, are calculated for all possible combinations of t and s $(t=1,2,\ldots,10$ and $s=t$, $t+1,\ldots,10)$. These are listed in Tables 5 and 6.

Using the backward dynamic programming optimization algorithm, the mini mum discounted cost and the optimum decision for system expansion are deter mined as follows:

(i) At the end of the planning period T=10, there is only one capacity to be considered, i.e., $X_{10,10}$ or 93,000 m³/day. The total discounted cost for this capacity is $C(X_{10, 10}) = SR 2500 \times 10^6$.

Hence

$$
f_{10}^*(x_{10,10}) = c(x_{10,10}) = 2500 \times 10^6
$$

For the 9th year, two alternatives are to be evaluated. These are mathematically represented as follows:

$$
f_{9}^{*}(X_{9,10}) = Min \begin{bmatrix} C(X_{9,9}) + (1+r)^{-1} f_{10}^{*}(D_{10}^{9} - X_{9,9}) \\ C(X_{9,10}) \end{bmatrix}
$$

= Min
$$
\begin{bmatrix} 2278 + (1.1)^{-1} \times 2500 = 4551 \\ or \\ 4023 \times 10^{6} \end{bmatrix} \times 10
$$

Hence the optimum decision is that a capacity of $175,000$ m³/day should be added at the beginning of year 9 to meet the demand up to the end of year 10. Its associated total discounted cost would be 4023 million Saudi Riyals.

Similarly, using the recurisive relationship of Equation (3), the optimum decisions for years $8,7,...,1$ are obtained. Table 7 lists the optimal expansion plan. From this table, the optimum solution for year 1 is the final solution to the present formulation which implies that in order to meet the total demand of 564,000 ${\rm m}^3/{\rm day}$ at the end of year 10, the capacity expansion should be done in two stages. In the first stage, it is necessary to install a plant capacity $(X_{1, 5})$ in the beginning of year 1 to meet demand through year 5. This capacity is $197,000 \text{ m}^3/\text{day}$. In the second stage, it is necessary to install a capacity $(X_{6, 10})$ in the beginning of year 6 to meet demand through year 10. This capacity would be $367,000 \text{ m}^3/\text{day}$. The total discounted cost for both stages would be 8767 million Saudi Riyals.

Year t	Optimum Expansion Plan	Discounted Total Cost (Million SR)
10	$f_{10}^{*}(X_{10,10})$	2500
9	f_{9}^{*} (x _{9,10})	4023
8	f_8^* $(X_{8,10})$	5220
$\overline{7}$	f_7^* $(x_{7,10})$	6201
6	f_6^* ($X_{6,10}$)	7028
5	f'_{5} ($X_{5,10}$)	7735
$\overline{4}$	f_4^* $(x_{4,7}) + (1+r)^{-4} f_8^*(x_{8,10})$	8250
3	f''_{3} (X _{3,6}) + (1+r) ⁻⁴ f''_{7} (X _{7,10)}	8502
$\overline{2}$	f_2^* (X _{2,6}) + (1+r) ⁻⁵ $f_7^*(X_{7,10})$	8685
$\mathbf{1}$	f_1^* (X _{1.5}) + (1+r) ⁻⁵ $f_6^*(X_{6,10})$	8767

TABLE 7 - DYNAMIC PROGRAMMING SOLUTIONS TO OPTIMUM EXPANSION OF DESALINATION PLANTS IN WESTERN REGION

CONCLUSIONS

The dynamic programming formulation presented in this study is a useful tool for water resources planners and decision makers in developing an optimal plan for increasing the desalination capacity in a given region over a given period of time and at a minimum cost. This formulation yields optimum capacity increments and the optimum period necessary for the expansion of a given system to meet future demands. Due to rapid industrialization and agricultural developments and also due to improvements in the standard of living, the future water demands in different regions can best be demonstrated by a simple exponential regression model. The criteria for optimization is to minimize the total discounted costs. Although the formulation presented in this study is an attempt towards its application in desalination expansion, it can be modified and applied for optimum conjunctive use of desalinated water along with other feasible water resource alternatives such as available ground and surface waters and water reclaimed from urban wastes. The effect iveness of this methodology in regional water resources planning depends upon the availability of data on capital, and operating costs for each alternative. A multi-decision stochastic dynamic programming optimization model can be formulated and the constraints on supply and demand with time can be defined for optimum water resources expansion.

REFERENCES

- [l] Abdul-Fatah, A.F., Husseiny, A.A., and Sabri, Z.A., 'Nuclear Desalina tion for Saudi Arabia: An Appraisal', Desalination, Vol. 25, pp. 163- 185, 1978.
- [2] Batanouny, K.H., 'Socio-economic Changes and Development of Water Resources in Saudi Arabia', Modelling, Identification, and Control in Environmental Systems, North Holland Publication, pp. 935-950, 1978.
- [3] Bellman, R., 'Dynamic Programming', Princeton University Press. Princeton, N.J. 1967.
- [4] Bogle, M.G.V., and O'Sullivan, M.J., 'Stochastic Optimization of Water Supply Expansion', Water Resources Research, Vol. 15, No. 5, pp. 1229- $1237, 1979.$
- [5] Butcher, W.S., Haimes, Y.Y., and Hall, W.A., 'Dynamic Programming Algorithm for the Optional Sequencing of Water Supply Projects', Water Resources Research, Vol. 5, No. 6, pp. 1196-1203, 1969.
- [6] Davis, R.S., and Meyerhoffer, S.J., 'Preliminary Report on the Water Resources of Najran Valley and Vicinity', Ministry of Agriculture and Water, Riyadh, 1957.
- [7] English, J.M., and El-Ramly, N., 'Economic Evaluation of Desalting Sub system as a Part of the Totoal Water System', Desalination, Vol. 3, pp. 308-317, 1967.
- [8] Hinomoto, H., 'Dynamic Programming of Capacity Expansion of Municipal Treatment Systems', Water Resources Research, Vol. 8, No. 5, pp. 1178- 1187, 1972. ' ll
- [9] Hughes, T.C., 'Optimal Capacity of Municipal Water Supply Pumps', Journal of the Water Resources Planning and Management Division, Proc. ASCE, Vol. 105, No. WR2, pp. 317-328, 1979.
- [10] Italconsult, 'Reports on Agricultural Resources Survey', prepared for the Ministry of Agriculture and Water, 1970-71.
- [11] Khatib, A.B., 'Seven Green Spikes', Water and Agriculture Development, Ministry of Agriculture and Water, Riyadh, 1974.
- [12] Larson, T.J., and Leitner, G., 'Desalting Seawater and Brackish Water: A Cost Update', Proc. International Congress on Desalination and Water Reuse, Nice, France, pp. 525-539, 1979.
- [13] Manne, A.S., 'Investment for Capacity Expansion', MIT Press, Cambridge, 1967.
- [14] Mawer, P.A., and Burley, M.J., 'The Conjuctive Use of Desalination and Conventional Surface Water Resources', Desalination, Vol. 4, pp. 141- $157, 1968.$
- [15] Morin, T.L., 'Optimal Sequencing of Capacity Expansion Projects', Journal of the Hydraulics Division, Proc. ASCE, Vol. 99, No. HY4 pp. 1605-1622, 1973.
- [16] Mishari, H., 'Towards Full Water Utilization in Saudi Arabia', Interna tional Conference on Water for Peace, Washington, D.C., 1969.

[17] Otkun, G., 'Outlines of Groundwater Resources of Saudi Arabia', Proc. International Conference on Arid Lands in Changing World, Tuscon, Arizona, 1969.

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- ,.[18] Scarato, R.F., 'Time-Capacity Expansion of Urban Water Systems', Water Resources Research, Vol. 5, No. 5, pp. 929-936, 1969.
- [19] 'Second Development Plan 1975-1980' Central Planning Organization, Riyadh, 1975.
- [20] 'Third Development Plan 1980-1985' Central Planning Organization, Riyahd, 1975.
- [21] Wojick, C.K., and Maadhah, A.G., 'Waters and Desalination Programs of Saudi Arabia', Journal of Water Supply Improvement Association, Vol. 8. No. 2, pp. 3-21, 1981.
- [22] Zukovs, G., and Adams, B.J., 'Capacity Expansion Planning Model for Wastewater Treatment and I/I Control', Water Resources Bulletin, Vol. 16, No. 4, pp. 601-607, 1980.